## Retirement Plan Investment \& <br> Risk Management Exam



Date: Friday, May 3, 2024

## INSTRUCTIONS TO CANDIDATES

## General Instructions

1. This examination has 6 questions numbered 1 through 6 with a total of 40 points.

The points for each question are indicated at the beginning of the question.
2. While every attempt is made to avoid defective questions, sometimes they do occur. If you believe a question is defective, the supervisor or proctor cannot give you any guidance beyond the instructions provided in this document.

## Written-Answer Instructions

1. Each question part or subpart should be answered either in the Word document or the Excel file as directed. Graders will only look at work in the indicated file.
a) In the Word document, answers should be entered in the box marked ANSWER. The box will expand as lines of text are added. There is no need to use special characters or subscripts (though they may be used). For example, $\beta_{1}$ can be typed as beta_1 (and $\wedge$ used to indicate a superscript).
b) In the Excel document formulas should be entered. Performing calculations on scratch paper or with a calculator and then entering the answer in the cell will not earn full credit. Formatting of cells or rounding is not required for credit.
2. The answer should be confined to the question as set.
3. Prior to uploading your Word and Excel files, each file should be saved and renamed with your fivedigit candidate number in the filename.
4. The Word and Excel files that contain your answers must be uploaded before time expires.

Chicago, IL 60631

## Navigation Instructions

Open the Navigation Pane to jump to questions.
Press Ctrl+F, or click View > Navigation Pane:

1.
(7 points) You are the actuary for a defined benefit pension plan with the following projected benefit payments. You are also given the yield curve.

| Time | Yield <br> Curve | Benefit <br> Payments | Time | Yield <br> Curve | Benefit <br> Payments | Time | Yield <br> Curve | Benefit <br> Payments |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | $1.50 \%$ | 967,095 | 26 | $1.75 \%$ | 871,622 | 51 | $3.00 \%$ | 955,005 |
| 2 | $1.50 \%$ | 994,926 | 27 | $1.75 \%$ | 827,808 | 52 | $3.00 \%$ | 915,916 |
| 3 | $1.50 \%$ | 870,820 | 28 | $1.75 \%$ | 959,335 | 53 | $3.00 \%$ | 803,525 |
| 4 | $1.50 \%$ | 984,790 | 29 | $1.75 \%$ | 809,492 | 54 | $3.00 \%$ | 973,959 |
| 5 | $1.55 \%$ | 919,110 | 30 | $1.80 \%$ | 838,542 | 55 | $3.00 \%$ | 939,004 |
| 6 | $1.60 \%$ | 890,197 | 31 | $1.90 \%$ | 916,880 | 56 | $3.25 \%$ | 967,848 |
| 7 | $1.60 \%$ | 904,429 | 32 | $2.00 \%$ | 818,693 | 57 | $3.25 \%$ | 884,740 |
| 8 | $1.60 \%$ | 942,606 | 33 | $2.00 \%$ | 967,286 | 58 | $3.25 \%$ | 963,081 |
| 9 | $1.60 \%$ | 877,937 | 34 | $2.00 \%$ | 825,890 | 59 | $3.25 \%$ | 860,740 |
| 10 | $1.62 \%$ | 992,304 | 35 | $2.00 \%$ | 830,582 | 60 | $3.25 \%$ | 897,475 |
| 11 | $1.62 \%$ | 865,967 | 36 | $2.25 \%$ | 834,384 | 61 | $3.50 \%$ | 811,559 |
| 12 | $1.62 \%$ | 951,575 | 37 | $2.25 \%$ | 820,906 | 62 | $3.50 \%$ | 933,811 |
| 13 | $1.65 \%$ | 906,064 | 38 | $2.25 \%$ | 900,586 | 63 | $3.50 \%$ | 936,642 |
| 14 | $1.65 \%$ | 851,085 | 39 | $2.25 \%$ | 885,231 | 64 | $3.50 \%$ | 979,822 |
| 15 | $1.65 \%$ | 861,298 | 40 | $2.50 \%$ | 952,161 | 65 | $3.50 \%$ | 874,361 |
| 16 | $1.65 \%$ | 921,309 | 41 | $2.60 \%$ | 905,709 | 66 | $3.50 \%$ | 883,417 |
| 17 | $1.70 \%$ | 854,977 | 42 | $2.75 \%$ | 894,265 | 67 | $3.50 \%$ | 958,052 |
| 18 | $1.70 \%$ | 991,782 | 43 | $2.75 \%$ | 940,201 | 68 | $3.50 \%$ | 819,937 |
| 19 | $1.70 \%$ | 917,077 | 44 | $2.75 \%$ | 875,739 | 69 | $3.50 \%$ | 861,836 |
| 20 | $1.75 \%$ | 856,812 | 45 | $2.75 \%$ | 975,753 | 70 | $3.50 \%$ | 805,696 |
| 21 | $1.75 \%$ | 956,826 | 46 | $2.75 \%$ | 824,537 | 71 | $3.50 \%$ | 995,377 |
| 22 | $1.75 \%$ | 883,498 | 47 | $2.75 \%$ | 809,369 | 72 | $3.50 \%$ | 957,163 |
| 23 | $1.75 \%$ | 987,016 | 48 | $2.75 \%$ | 854,715 | 73 | $3.50 \%$ | 830,089 |
| 24 | $1.75 \%$ | 941,036 | 49 | $2.75 \%$ | 899,690 | 74 | $3.50 \%$ | 944,436 |
| 25 | $1.75 \%$ | 820,739 | 50 | $2.75 \%$ | 938,714 | 75 | $3.50 \%$ | 860,574 |
|  |  |  |  |  |  |  |  |  |

(a) (2 points) Calculate the duration of the liabilities of the pension plan.

The response for this part is to be provided in the Excel spreadsheet.

## 1. Continued

You are given the liability impact for the following shifts in the yield curve:

|  | D1 | D2 | D3 | Liability <br> Impact |
| :--- | :--- | :--- | :--- | :--- |
| Shift 1 | + +100bps | +50 bps | 0 | $-\$ 528,000$ |
| Shift 2 | +75 bps | -75 bps | 0 | $+\$ 792,000$ |

(i) The market value of the pension plan's fixed income investment is \$8,800,000.
(ii) The effective duration of the fixed income investment is equal to the effective duration of the liabilities.
(iii) The pension plan is fully immunized against shifts in the yield curve.
(b) (3 points) Calculate key-rate durations D1, D2 and D3 for the fixed income investment.

The response for this part is to be provided in the Excel spreadsheet.
(c) (2 points) Describe the challenges associated with a cash flow matching strategy.

ANSWER:
2.
(6 points)
(a) (1 point) Compare and contrast the calculation of market liability and budget liability from the financial economics perspective for the following two assumptions:
(i) Default rate
(ii) Discount rate

## ANSWER:

(b) (5 points) Compare and contrast the calculation of market liability and budget liability from the financial economics perspective for the following:
(i) Interest rate risk
(ii) Credit risk
(iii) The pursuit of alpha

## ANSWER:

## 3.

(7 points) You are the actuary for Company ABC's defined benefit pension plan. Company ABC recently made the decision to terminate the plan within 5 years. The primary objective of Company ABC is to minimize the cost of plan termination by ensuring that the plan is fully funded before termination occurs.

You are given:

| Plan type | Closed and frozen |
| :--- | :--- |
| Funded status | $86 \%$ |
| Asset allocation | $60 \%$ equity / 40\% bonds |
| Bond duration | 7.2 years |
| Liability duration | 9.8 years |

(a) (2 points) Describe the benefits of implementing a glide path liability-driven investment (LDI) strategy.

## ANSWER:

(b) (5 points) Recommend one of the following LDI strategies considering Company ABC's primary objective.

Justify your recommendation.

|  | Option 1 | Option 2 |
| :--- | :--- | :--- |
| Initial asset allocation | No immediate change | $35 \%$ Equity / <br> $65 \%$ Bonds |
| Triggers | Interest rate level <br> (long term bond index) <br> increases by 0.50\% | Funded status <br> improves by 2\% |
| Monitoring frequency | Quarterly | Monthly |
| \% of equity replaced <br> with bonds when a <br> trigger is reached | $15 \%$ | $5 \%$ |
| Duration of bonds <br> added to the portfolio | 14.9 years | 7.2 years |
| End state objective | Hedge ratio $=100 \%$ | Funded status = 100\% |

## ANSWER:

4. 

(9 points)
(a) (2 points) List the four main objectives of performance measurement tools.

ANSWER:
(b) (3 points) Identify the strengths and weaknesses of using risk-adjusted return ratios for performance measurement.

ANSWER:

You are given the following information on three portfolios:

| Portfolio 1 |  |  |  | Portfolio 2 |  |  |  | Portfolio 3 |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | MV0 | 750 |  |  | MV0 | 225 | Beginning of year MV |  |  | 1000 |
| CF1 | 100 | MV1 | 975 | CF1 | 50 | MV1 | 320 | CF1 | 100 | MV1 | 1140 |
| CF2 | 75 | MV2 | 1000 | CF2 | -60 | MV2 | 260 | CF2 | -40 | MV2 | 1250 |
| CF3 | 100 | MV3 | 1000 |  |  |  |  | CF3 | 225 | MV3 | 1480 |
| CF4 | 50 | MV4 | 1225 |  |  |  |  | CF4 | 80 | MV4 | 1370 |
|  |  |  |  |  |  |  |  | CF5 | -50 | MV5 | 1290 |
|  |  |  |  |  |  |  |  | CF6 | 100 | MV6 | 1400 |
|  |  |  |  |  |  |  |  | CF7 | -30 | MV7 | 1390 |
|  |  |  |  |  |  |  |  | CF8 | 0 | MV8 | 1500 |
|  |  |  |  |  |  |  |  | CF9 | 100 | MV9 | 1625 |
|  |  |  |  |  |  |  |  | CF10 | 250 | MV10 | 1750 |
|  |  |  |  |  |  |  |  | CF11 | 300 | MV11 | 1875 |
|  |  |  |  |  |  |  |  | CF12 | 0 | MV12 | 2000 |
|  |  |  |  |  |  |  |  | End of year MV |  |  | 2045 |


| Portfolio 1 | Cash flows (CF) \& market values (MV) are quarterly at the end of the <br> quarter |
| :--- | :--- |
| Portfolio 2 | Cash flows \& market values are semi-annual at the end of the period |
| Portfolio 3 | Cash flows \& market values are monthly, mid-month |

Market values shown are inclusive of cash flows at the valuation date.
(c) (3 points) Calculate the dollar-weighted and time-weighted rates of return for each of the three portfolios.

The response for this part is to be provided in the Excel spreadsheet.

## 4. Continued

(d) (1 point) Calculate the Sharpe Ratio for portfolios 1 and 2 assuming a risk-free rate of $2.50 \%$ and using the time-weighted return calculated in c) above.

The response for this part is to be provided in the Excel spreadsheet.

## 5.

(5 points)
(a) (3 points) Describe the considerations when defining a public pension plan's objectives for the purpose of establishing a risk management framework.

## ANSWER:

(b) (2 points) Describe the factors that contribute to distortions in the feedback loop for public pension plans.

## ANSWER:

6. 

(6 points) Company XYZ is a large petroleum firm that has recently hired you, a pension actuary, to review the investment practices in their two defined benefit pension plans for their Division A and Division B employees, respectively.

|  | Division A | Division B |
| :--- | :--- | :--- |
| Plan type | Closed | Open |
| Plan participants | $30 \%$ actives and 70\% retirees | $70 \%$ actives and 30\% retirees |
| Plan assets | $\$ 850$ Million | $\$ 600$ Million |
| Plan liabilities | $\$ 700$ Million | $\$ 800$ Million |

You are given the following excerpt of the Statement of Investment Policies and Procedures (SIPP) applicable for both Division A and Division B plans.

| Investment <br> objectives | - Minimize sponsor contributions and funding volatility on a <br> company level <br> Improve balance sheet and income statement of Company <br> XYZ |
| :--- | :--- |
| Investment <br> strategies | - Diversify investments by investing in stocks, bonds, and <br> alternative investments |
|  | Invest a proportion of stocks and bonds into the petroleum <br> industry <br> - Invest in residential and commercial real estate through the <br> purchase of exchange traded funds |
| - Invest in long-short style hedge funds to generate additional |  |
| return |  |
| - Duration match bonds on an aggregate company level |  |

6. 

Continued
(a) (4 points) Critique the elements provided above of Company XYZ's SIPP.

ANSWER:

Company XYZ is considering hiring an outsourced chief investment officer (OCIO) for both Division A and Division B plans.
(b) (2 points) Describe the advantages and disadvantages of the above consideration.

ANSWER:
**END OF EXAMINATION**

