of Nuclear Holocaust Hazard

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ABSTRACT

In a paper presented to the Twenty-Second Actuarial Research Conference, held last year at the University of Toronto, a notation and mathematical model were developed to explore the impact of nuclear holocaust hazard on actuarial mathematics. The purpose of the present paper is to consider this hazard in relation to long-term income maintenance systems such as Social Security and retirement plans.

The paper begins with a brief recollection of the notations used in the Toronto paper. It then highlights the actuarial projections of the 1988 Annual Report of the Board of Trustees of U.S. Old-Age and Survivors Insurance and Disability Insurance Trust Funds. These are very large systems with current annual outgo of \$220 billion, and rapidly growing assets. Under the less optimistic of two intermediate projections, the combined trust funds are estimated to reach a level of \$12 trillion by the end of 2030. Thereafter, the funds are projected to decline rapidly to exhaustion by 2050. A simple difference equation, in the notation of the Toronto paper, is examined as a possible means of controlling the upward and downward changes in the trust funds if Congress periodically adjusts OASDI financing to satisfy the equation.

Next sections of the paper consider what recognition of nuclear holocaust hazard would mean for pension mathematics. The easiest situation to discuss is in regard to reserves for retired members and beneficiaries. A second matter is the calculation of optional retirement annuities, and could entail much numerical work. The funding for active members will bring up many questions, in particular, in regard to the actuarial assumptions.

In concluding sections, the paper attempts to measure the scientific worth of recognizing nuclear holocaust hazard in our actuarial mathematics, and the consequences thereof. One keeps coming back to the idea that the only practical way to recognize such hazard is by a specific component of the interest rate. Thereby, long-term financial transactions can proceed quite logically even in the presence of the hazard. But one essential step for world progress is to minimize nuclear holocaust hazard. To aid this process, actuarial science should seek its truths, and communicate them widely. My initial efforts to do so, and possible activities for others, conclude the paper.

1. Introduction

In a paper, [1], presented to the 22nd Actuarial Research Conference, I set up notations and a mathematical model for considering the recognition of nuclear holocaust hazard in the actuarial mathematics for an individual "life aged x years", the phrase in quotation marks being denoted by (x). Here, we recall briefly those notations for subsequent use in regard to actuarial projections for Social Security, on an aggregate rather than individual basis, and for some aspects of pension mathematics.

We consider various consecutive years, (k,k+1), each specified by its beginning and ending times. By $v_1(k,k+1)$, we denote the present value at time k of 1 due at time k + 1, if ordinary discount

(interest-in-advance) for the year is at annual rate $d_1(k)$. Then,

$$v_1(k,k+1) = 1 - d_1(k)$$
, (1.1)

and the corresponding effective annual rate of interest-in-arrears is

$$i_1(k+1) - d_1(k)/v_1(k,k+1)$$
 (1.2)

A further notation is

$$v_1(h,k) = \frac{k-1}{g-h} v_1(g,g+1)$$
 (1.3)

for the present value at time h of 1 due at time k if discount rates are $d_1(g)$, g = h, h + 1,..., k - 1.

The annual discount rate for nuclear holocaust hazard was denoted by $d_2(k)$, and

$$v_{2}(k,k+1) = 1 - d_{2}(k)$$
 (1.4)

Then,

$$v_2(h,k) = \frac{k-1}{g-h} v_2(g,g+1)$$
 (1.5)

discounts to time h a unit due at time k for nuclear holocaust in the interval (h,k), such holocaust not having occurred before time h.

Also defined were composite factors

$$v_{1,2}^{(k,k+1)} = v_1^{(k,k+1)}v_2^{(k,k+1)}$$
 (1.6)

$$d_{1,2}^{(k)} - 1 - v_{1,2}^{(k,k+1)}$$

- $d_1^{(k)} + d_2^{(k)} - d_1^{(k)} d_2^{(k)}$. (1.7)

For calculations pertaining to (x) , we introduced the annual rate of mortality $d_3^{(k)}$ - $q_{x+k}^{}$, and

$$v_3(k,k+1) = 1 - d_3(k) = p_{x+k}$$
 (1.8)

One can form composite factors, such as $v_{1,3}(k,k+1) - v_1(k,k+1)v_3(k,k+1)$, similarly $v_{1,3}(h,k)$, $v_{2,3}(h,k)$ and $v_{1,2,3}(h,k)$. Many relations follow therefrom. In particular, the net single premium for a whole life insurance of 1 payable at the end of the year of death of (x) if nuclear holocaust has not intervened is

$$A_{1,2,3}(0,\omega-x) = \sum_{k=0}^{\omega-x-1} v_{1,2}(0,k+1)v_3(0,k)d_3(k) . \qquad (1.9)$$

Also, the actuarial present value of a unit life annuity-due to (x), with recognition of nuclear holocaust hazard, is

$$\ddot{a}_{1,2,3}^{(0,\omega-x)} = \sum_{k=0}^{\omega-x-1} v_{1,2,3}^{(0,k)} . \qquad (1.10)$$

Analogous to the relation, $1 - d\ddot{a}_{y} + A_{y}$, one can show that

$$\sum_{k=0}^{\omega-x-1} d_{1,2}(k)v_{1,2,3}(0,k) + A_{1,2,3}(0,\omega-x) - 1$$
(1.11)

by algebra or general reasoning (see formulas (5.1) and (6.3) of [1]). Also,

$$\sum_{k=0}^{\omega-x-1} d_1^{(k)v_{1,2,3}^{(0,k)} + A_{1,2,3}^{(0,\omega-x)}}$$

$$-\sum_{k=0}^{\omega-x-1} d_{1,2}(k)v_{1,2,3}(0,k) + A_{1,2,3}(0,\omega-x) + \sum_{k=0}^{\omega-x-1} \left[d_{1}(k) - d_{1,2}(k) \right] v_{1,2,3}(0,k) - 1 - \sum_{k=0}^{\omega-x-1} d_{2}(k)v_{1}(k,k+1)v_{1}(0,k)v_{2,3}(0,k)$$

[by use of (1.11) , (1.7) and (1.1)]

$$-1 - \sum_{k=0}^{\omega-x-1} v_1(0,k+1)v_{2,3}(0,k)d_2(k) . \qquad (1.12)$$

Here, the last summand represents the actuarial present value of the death claim payment lost in year (k+1) by reason of nuclear holocaust in the year.

You will have observed that discount notations, d and v, have been used for ordinary interest, nuclear holocaust, and mortality. Each of the corresponding rates operates in a distinctive way, different from that of the others. Nevertheless, there is a great deal of symmetry in the mathematical formulas such as (1.6), (1.7) and (1.10), but less in formulas such as (1.9) and (1.12). The theory can be enriched by probability interpretations but for this paper discount interpretations are appropriate.

2. OASDI Actuarial Projections

We start by highlighting the projected financing of Old-Age, Survivors and Disability Insurance (OASDI) in the United States. Short-range and long-range actuarial projections are contained in the reports of the Board of Trustees, and we shall refer to those in the 1988 report, [2]. For these projections, four alternative sets of demographic, economic and programmatic assumptions are utilized with Alternative I labeled as "optimistic" and Alternative III as "pessimistic". Alternatives II-A and II-B are labeled "intermediate". They share the same demographic assumptions but II-A assumes more robust economic growth than II-B. This carries implications over to the programmatic assumptions and bases (see [3] Andrews-Beekman).

Various measures of actuarial status are used, [2], [4]. <u>Contingency</u> <u>fund ratio</u> is the amount in the trust fund at the beginning of the year, including advance transfers for January, divided by that year's expenditures. This measure is used extensively for the short-range projections.

Chart A (from the Report) shows the OASDI contingency fund ratio for 1988, 41 percent, and the projected OASDI ratios for 1989-93, on the basis of all four sets of assumptions. Alternative II-B shows a 1992 ratio in excess of 100 percent.



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In regard to the long-range projections, we have the statements: "In analyzing the actuarial status of OASDI for the next 75 years, several different measures are commonly used. The <u>income rate</u> is the combined OASDI employee-employer contribution rate scheduled in the law, plus the income from taxation of benefits, expressed as a percentage of taxable payroll. The <u>cost rate</u> is the annual outgo expressed as a percentage of taxable payroll."

It is important to note that Trust Fund investment income is not included in the income rate.

Figure 2 (from the Report) exhibits the cost rates for each of the four Alternatives; and the income rates which do not vary much by alternative (cf. [2], Table 26.). An excess of income for the next 25 years is indicated for all four Alternatives. If, however, contingency fund ratios are considered, we observe from Figure 4 (of [2]) that the ratio peaks about 2010 at less than 2.5 for Alternative III, at 5.3 in 2015 for Alternative II-B, and soars to more than 13 under optimistic Alternative I.

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Calendar Year

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Another quotation from [2], with a parenthetical comment is:

"For this report, long-range <u>actuarial balances</u> are calculated using "level-financing" methodology. (Thereby, equivalent level percentages of future increasing taxable payroll replace the year-by-year income and cost rates, and the actuarial balance is the difference between the level percentages.) The methodology discounts future surpluses and deficits using the <u>real</u> rate of interest. It is the most appropriate for summarizing the financial status of the OASDI system over the 75-year period, a period in which the trust funds build up in the early years when income exceeds outgo and are subsequently depleted during the final years when expenditures are expected to exceed income".

The following table, a portion of Table 27 of [2], presents actuarial balances as defined above.

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TABLE 1

OASDI ACTUARIAL BALANCES BY ALTERNATIVE, 1988-2062

(As a percentage of taxable payroll)

	Equivalent Level Income Rate*	Equivalent Level Cost Rate	Actuarial Balance
Alternative I	10 7/	0.51	3 34
25 years: 1966-2012	12.74	9.51	5.24
50 years: 1988-2037	12.80	10.57	2.23
75 years: 1988-2062	12.83	10.97	1.86
Alternative II-A			
25 years: 1988-2012	12.77	10.14	2.63
50 years: 1988-2037	12.85	11.77	1.08
75 years: 1988-2062	12.91	12.83	.08
Alternative II-B			
25 years: 1988-2012	12.78	10.54	2.24
50 years: 1988-2037	12.87	12.34	. 53
75 years: 1988-2062	12.94	13.52	58
Alternative III			
25 years: 1988-2012	12.82	11.72	1,11
50 years: 1988-2037	12.95	14.23	-1.28
75 years: 1988-2062	13.07	16.49	-3.42

*Income rates take account of the beginning trust fund.

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We conclude these highlights of [2], with a reference to its Appendix G - Long-Range Estimates of Social Security Trust Fund Operations in Dollars. The Appendix notes that long-range trust fund operations are not usually shown in dollar amounts because inflation makes such amounts non-comparable over time. Measures such as cost rates and income rates, expressed as percentages of taxable payroll, are more stable. Demand exists, however, for long-range dollar values, and these are presented together with sets of indices that may be used to deflate the magnitude of future dollar items.

A sample of such dollar amounts is given in Table 2.

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TABLE 2

Estimated Operations of OASDI TRUST FUND [Alternative II-B, in billions]

Calendar Year	Income Excluding Interest	Interest	Total Income	Total Outgo	Assets at End of Year
1990	293.3	16.3	309.5	252.2	211.9
2000	547.9	83.6	631.5	446.8	1,409.4
2015	1,302.6	383.7	1,686.3	1,203.7	6,763.0
2030	2,898.7	692.0	3,590.7	3,524.5	11,837.5
2045	6,422.5	251.8	6,674.3	7,966.8	3,799.4

Thereafter, action required to avoid exhaustion.

Figures such as these were undoubtedly the source of the April 11, 1988 New York Times perceptive editorial "Trillions, Trillions All Around".

3. Levers for Controlling the Level of the OASDI Trust Fund

It is clear from the foregoing discussion of [2], that the OASDI Trust Fund will, under present law, increase rapidly over the next two decades. but later will reach a maximum and decrease rapidly. One is reminded of various papers concerned with funding equilibria that appear in long-term stable benefits programs, [5], [6]. For the immediate future of the OASDI Trust Fund, these appear to offer little guidance. Eventually, some mathematical discussion of benefit outgo and tax income may be enlightening. Another source is J. R. Trowbridge's paper, [7], in regard to the assessment systems that have emerged in France. One gathers that benefits are expressed in terms of units whose value is adjusted as financial resources require, thus achieving actuarial equilibrium. Again, there may be ideas to be gained from this approach but their implementation would seem to require a massive restructuring of OASDI, with all the consequent debate and persuasion that would be entailed. It appears simpler to work within the present structure, particularly in terms of the short-range projections. In the following proposal for providing actuarial-financial control of OASDI, we shall also recognize nuclear holocaust hazard.

For this purpose, the following notations will be used:

- F(k) the value in dollars of the OASDI Trust Fund at time k , ignoring, for simplicity, details such as advance transfers from the Treasury.
- I(k) the value at time k of projected income for year (k,k+1), exclusive of interest.
- O(k) = the value at time k of projected outgo for the year
 (k,k+1).

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Then, if $i_{1,2}(k+1)$ is the effective annual rate of interest, equivalent to $d_{1,2}(k)$, the composite rate of discount based on $d_1(k)$ and $d_2(k)$ defined in section 1, we have

$$\left[F(k) + I(k) - O(k)\right] \left[1 + i_{1,2}(k+1)\right] - F(k+1) . \quad (3.1)$$

Because we ignore advance transfer payments, we shall consider the <u>fund ratio</u> [F(k)/O(k)] rather than the Report's contingency fund ratio. Suppose now that at time k, the fund ratio is c, that is, F(k) - c.O(k), and that we wish to maintain the ratio at that level. From (3.1), we require

$$\left[(c-1)0(k) + I(k) \right] - v_{1,2}(k,k+1) \left[c \cdot 0(k+1) \right]$$

or

$$I(k) = v_{1,2}(k,k+1)[c \cdot 0(k+1)] - (c-1) \cdot 0(k)$$
 (3.2)

In particular, for the frequently recommended case, c = 1,

$$I(k) = v_{1,2}(k,k+1)O(k+1)$$
 (3.3)

If nuclear holocaust hazard were negligible, (3.3) would become $I(k) = v_1(k,k+1)O(k+1) . \text{ If nuclear holocaust hazard is not negligible,}$ then $v_{1,2}(k,k+1) = v_1(k,k+1).v_2(k,k+1) < v_1(k,k+1)$. It appears that the presence of nuclear holocaust hazard reduces the cost of maintaining the fund ratio at a level of 1. By substituting $v_1(k,k+1) \begin{bmatrix} 1 & d_2(k) \end{bmatrix}$ for $v_{1,2}(k,k+1)$, we can rewrite (3.3) as

 $I(k) = v_1(k,k+1)O(k+1) - d_2(k)v_1(k,k+1)O(k+1) . \quad (3.4)$ The term $d_2(k)v_1(k,k+1)O(k+1)$ states explicitly the afore-mentioned cost reduction when nuclear holocaust hazard is recognized.

The situation is, however, very complex and can be evaluated accurately only as experience unfolds. The presence of nuclear holocaust hazard over a period of years may influence fertility rates, and entail the

consequences thereof. As discussed in [1], nuclear holocaust hazard can have a drastic impact on survival rates. Also, interest rates may be higher by a nuclear holocaust component. A warning should be sounded here: one must avoid duplicate recognition. If nuclear holocaust hazard is recognized in the assumed interest rates, then survival rates should be taken from the usual sources. Other assumptions that nuclear holocaust may modify are wage increase rates, consumer price increases, unemployment rates, and indeed general morale ranging from bleak pessimism to constructive hope based on intelligent and informed actions to deal with the hazard. By constant observation and analysis, trends can be recognized and incorporated into the actuarial projections, and the results evaluated.

Returning to (3.3), let us consider how it may be used to maintain the fund ratio at a level of 1, that is, at 100 percent. Currently, that ratio is increasing toward 100 percent. When it reaches that level in the early 1990's, it is within Congress' power to maintain it there by increasing outgo, 0(k+1), or decreasing income, I(k), or by some combination thereof. In view of the long-range projections, and the projected ultimate exhaustion of the fund if tax rates remain unaltered, such increase of outgo would be unwise.

Decreasing income by temporary decrease in the OASDI tax rates would be reasonable, and should be done periodically in the light of the short-range projections and (3.3). This would still permit a large dollar fund to accumulate, as can be seen from the outgo column of Table 2, and recalling that (3.3) requires the fund at time k to be equivalent to O(k+1), the value at time k + 1 of the outgo for year (k+1,k+2). Such a fund should suffice to quell the anxiety of future beneficiaries as to

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whether money will be available when their benefits come on stream.

Fairly early in the next century if OASDI tax rates have been reduced, there will be a funding turn around, tending to decrease the fund ratio below 100 percent. At that time, and at subsequent times thereafter, it may be necessary for Congress to restore tax rates to previously legislated levels, and in the longer term, to increase them further if the fund ratio is to be maintained at 100 percent. This will increase I(k) . An alternative lever, which like the tax increase, would engender opposition, consists of Congress decreasing the benefit outgo, the main element of O(k+1), by modification or postponement of increases in proportion to the Consumer Price Index. A precedent for postponement has been established already by the 1983 Amendments.

Still a third lever to be used when the fund ratio is under pressure is for Congress to increase the taxation of Social Security incomes, and thereby increase I(k). Again, a precedent for this action has been established by the 1983 Amendments.

With these powerful levers available to it, the Congress can, if it wills, maintain the fund ratio at the reasonable level of 100 percent. These levers are known, and all have been used before. But both the public and the Congress should become familiar with them, and expect their use when from time to time circumstances may require their application.

4. Retired Member Pension Reserves

It is relatively easy to discuss the effect of recognizing nuclear holocaust hazard in reserves for retired members and their beneficiaries under a given pension plan. For this purpose, we begin with the recursion formula (6.4) of [1], namely,

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$$\ddot{a}_{1,2,3}(k,\omega-x) = 1 + v_{1,2,3}(k,k+1)\ddot{a}_{1,2,3}(k+1,\omega-x) . \quad (4.1)$$

On substituting $v_{1,3}(k,k+1)\left[1 - d_2(k)\right]$ for $v_{1,2,3}(k,k+1)$, we obtain

Multiplication by $v_{1,3}(0,k)$ and summation over k gives

$$\overset{a_{1,2,3}(0,\omega-x)}{\overset{\omega-x-1}{\underset{k=0}{\overset{\omega-x-1}{\overset{(0,\omega-x)}{\overset{(0,k+1)a_{1,2,3}(k+1,\omega-x)}{\overset{(0,k+1,\omega-x)}{\overset{(4.2)}}{\overset{(4.2)}{\overset{(4.2)}{\overset{(4.2)}{\overset{(4.2)}{\overset{(4.2)}{\overset{(4.2)}{\overset{(4.2)}{\overset{(4.2)}{\overset{(4.2)}{\overset{(4.2)}{\overset{(4.2)}{\overset{(4.2)}{\overset{(4.2)}}{\overset{(4.2)}{\overset{(4.2)}}{\overset{(4.2)}{\overset{(4.2$$

Here, $\ddot{a}_{1,3}(0,\omega-x) = \ddot{a}_x$ based on ordinary interest and mortality. Thus, the actuarial present value for a life annuity with recognition of nuclear holocaust hazard is less than the usual actuarial present value by the additional reserves deleted by nuclear holocaust hazard.

A slightly different view is given by arranging (4.2) as

$$\ddot{a}_{1,2,3}^{(0,\omega-x)} + \sum_{k=0}^{\omega-x-1} d_2^{(k)v_{1,3}^{(0,k+1)}} \dot{a}_{1,2,3}^{(k+1,\omega-x)} - \ddot{a}_{1,3}^{(0,\omega-x)} .$$
(4.3)

Here, (4.3) asserts that the reserve $a_{1,2,3}(0,\omega-x)$, recognizing nuclear holocaust hazard, plus the present value of the discounts at rate $d_2(k)$ on the reserve expected to be required at time k + 1, k = 0, 1,..., $\omega - x - 1$, suffice to provide the ordinary life annuity reserve, $a_{1,3}(0,\omega-x)$. The redundancy in exposition here is deliberate. In (4.2), one views nuclear holocaust as a cataclysmic contingency, while in (4.3) one asserts that in practice it may be taken into account as a special factor in the interest assumption. In either case, one sees that $a_{1,2,3}(0,\omega - x)$ is less than $a_{1,3}(0,\omega - x)$ by an amount depending on $d_2(k)$, $k = 0, 1, ..., \omega - x - 2$ (since the summand at $\omega - x - 1$ is zero). Thus, pension fund reserves for retirees and beneficiaries will be smaller if nuclear holocaust hazard is duly recognized.

One might also recognize nuclear holocaust hazard by using $v_{2,3}(k,k+1)$, the composite survival rate for year (k,k+1), but this does not provide a means for offsetting annuity losses when nuclear holocaust does not occur. Recognition of nuclear holocaust by an interest component is more feasible. To clarify this, one can rewrite (4.1) as

Formula (4.4) asserts that the annuity reserve at time k (with recognition of nuclear holocaust hazard) plus supplementary interest-in-advance $d_2(k)$ on $\alpha = v_{1,3}(k,k+1)a_{1,2,3}(k+1,\omega-x)$ provides the payment of 1 due at time k plus the amount α needed to provide the annuity reserve at time k + 1.

A final comment is that if retirement incomes are indexed, some additional consideration may be necessary. Such indexing is often restricted, so that the income increases can be predetermined, at least approximately.

5. Optional Annuities at Retirement

In many cases, pensions are not paid on a straight life annuity basis. Instead, a variety of optional annuities are available which may involve a period certain, or the survival of a second life. For simplicity of notation, we consider the optional annuity form providing for an annuity-certain for n years and for life thereafter so long as (x)

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survives. The conversion factor, for annual payment annuities-due, with recognition of nuclear holocaust hazard, is

$$\frac{\overset{a_{1,2,3}(0,\omega-\mathbf{x})}{\dots}}{\overset{a_{1,2,3}(0,n)}{\dots} + v_{1,2,3}(0,n)\overset{a_{1,2,3}(n,\omega-\mathbf{x})}{\dots}}$$
(5.1)

How this factor, and similar factors for other optional annuity forms, vary with degree of nuclear holocaust hazard assumed, could require extensive numerical calculation. The results would be related to those based on increasing the interest rate assumption but the latter might be on a more constant rather than year-by-year varying basis.

6. Pension Funding for Active Members

A full scale investigation of how nuclear holocaust hazard might be recognized in pension funding for active members could be very extensive, and has not been undertaken here. Brief consideration of how the actuarial assumptions might be influenced by such recognition will be the extent of this section.

There have been repeated statements that the practical way of recognizing nuclear holocaust hazard in long-term financial transactions is by composition with the rate of interest (investment return). This increases the interest rates assumed, and thereby increases accumulations under defined contribution plans and lowers costs under defined benefit plans.

The retirement rates assumed have significant impact on the funding costs of defined benefit pension plans. Over a long-term, members' apprehension of nuclear holocaust might lead to more early retirements.

Another significant assumption for pension funding costs is salary increase rates which often have price increases as a major component. The

long-term impact of recognizing nuclear holocaust hazard might well involve increasing trends for salaries and prices.

For active members, the effect of recognizing nuclear holocaust hazard is uncertain. The ready answer is that, viewed as a discount cause, nuclear holocaust hazard should reduce pension funding costs for active members of a defined benefit plan. But over a long-term, there may be unfavorable changes in other valuation factors, such as retirement rates, or salary increase rates, and these may offset the discount effect of the hazard.

7. Is This True Actuarial Science?

In his address to the Annual Actuarial Research Conference, at the University of Manitoba, the recently deceased Edmund C. Berkeley gave as his Proposition 10:

> "It is not right for actuaries and managers in insurance companies to exclude the risks of nuclear weapons, nuclear fission energy, war, and genocide in (a) policy contracts, (b) thinking and discussion, and (c) political and professional action." [8]

The part of this proposition that relates to nuclear holocaust has been growing in my mind since then.

In [1] and this paper we have worked with the discount factors

$$\mathbf{v}_{1,2,3}^{(k,k+1)} - \mathbf{v}_{1}^{(k,k+1)} \mathbf{v}_{2}^{(k,k+1)} \mathbf{v}_{3}^{(k,k+1)}$$

$$- \left[1 - d_{1}^{(k)}\right] \left[1 - d_{2}^{(k)}\right] \left[1 - d_{3}^{(k)}\right]$$

$$- \frac{1}{\left\{\left[1 + i_{1}^{(k+1)}\right] \left[1 + i_{2}^{(k+1)}\right] \left[1 + i_{3}^{(k+1)}\right]\right\}}$$

By making various combinations of the factors, and by summation, one gets

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all sorts of meaningful relations. For the present paper, because we have been thinking mainly about projected aggregate cash flows, discount notations and interpretations seem appropriate. But, as indicated in [1], in regard to individual lives, there is also much probability theory to explore. The actuarial mathematics with recogniztion of nuclear holocaust hazard rings as true as any of our more standard models. It allows many illuminating interpretations. Thereby, we get closer to the truth of our time.

I am convinced, however, that the world cannot, and will not, tolerate a significant level of nuclear holocaust hazard for an indefinite period of time. Thus, actuarial science with recognition of nuclear holocaust hazard should not be the ultimate mathematical basis for our insurance and benefit systems. But actuarial science has an immediate, supreme responsibility which it has been slow to assume, to demonstrate how nuclear holocaust hazard can impair all our financial security systems, and survival itself. Thereby, actuarial science could hasten the day when nuclear holocaust hazard will be a negligible factor, and can once again be ignored properly in actuarial calculations. The models developed on the way may then prove useful in other life-threatening circumstances.

In the next section, some of the immediate steps in the educational process of recognizing nuclear holocaust hazard are indicated.

8. Demonstrating the Actuarial Impact of Nuclear Holocaust Hazard

Emerging from the Toronto paper [1] are two main ideas. One concerns the impact of nuclear holocaust hazard on measures of survival such as expectation of future life and median survival age. These measures are understood imperfectly by the public, and in the current presence of

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nuclear holocaust hazard are in many presentations quite misleading. Actually, great real progress in public health, as calculated by improvements in such measures, could be accomplished through minimizing nuclear holocaust hazard.

The second main idea is that in the current world, all long-term financial payments should be discounted for nuclear holocaust hazard, and this is a practical way to incorporate the hazard into actuarial calculations. This second idea has been pursued in this paper in relation to actuarial projections for Social Security, and to some aspects of pension funding mathematics.

Portions of the Toronto paper were presented to the Research Club of The University of Michigan, once the soul of research at Michigan. An afternoon setting, preceded by sherry, and in a room darkened for slides, was conducive to slumber. Some members, including a past president of the American Statistical Association, evinced interest and may follow up the ideas. I now find myself on the Council of the Research Club, and hope to share ideas with concerned scientists in other units of the University.

Also, I recently corresponded with Dr. Helen Caldicott, a founder of Physicians for Social Responsibility, and the founder of Women's Action for Nuclear Disarmament (WAND). From Australia she wrote:

> "I find your work quite fascinating and a novel approach to getting people to think about the risks of nuclear holocaust. Indeed, I think it should be applicable to insurance companies throughout the world, and I find it fascinating to speculate, as have you, that the rising interest rates are a product of the innate risk and recognition of nuclear war."

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I plan to continue contacts with WAND, and may go on to communication with other national organizations such as Beyond War and the Union of Concerned Scientists.

Much work could be done on alternative models incorporating nuclear holocaust hazard, such as fully continuous models, and various types of multiple decrement models (cf. [9]; [10], Ch. 9). That work, together with supporting illustrations, could strengthen actuarial statements concerning nuclear holocaust hazard. But it would involve mainly communicating among ourselves, and it seems more urgent that we now communicate to others. The level of nuclear holocaust hazard is largely unknown, but a range of alternative assumptions concerning such level allows one to proceed. There is much opportunity for actuarial researchers and teachers to contribute to theory recognizing nuclear holocaust hazard. I hope that you will find such opportunity in your own organizations.

My final observation is that life insurance has been barely touched on in [1], and I have not discussed partial nuclear holocaust which may require more mathematical apparatus than the extreme case of total holocaust.

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ADDENDUM

Here I make a few comments on the reactions I have received recently on [1] and the current paper.

To me, one of the most important, but also most obvious, idea is that nuclear holocaust hazard, even of small degree, can over a lifetime substantially decrease measures of survival. I am surprised that pediatrician, Helen Caldicott, chose to comment on financial rather than survival effects, but the former may have been a new insight for her, while the latter has been of concern to her for many years.

As a test of ideas, in the current paper I look at financial effects as related to Social Security and pension systems. In response, C. L. Trowbridge has given an alternative view of current cost financing (cf. TSA 25(1973), p. 672). He also notes some additional levers, beyond those mentioned in the paper, that Congress might employ to keep Social Security income and outgo in appropriate balance. He states that nuclear holocaust hazard is not the only means by which humankind might self-destruct, and that the basic problem is how humans can cope with technological change.

R. J. Myers drew my attention to his paper "Future Financing Problems of National Pension Systems Can Be Avoided, Automatically", presented to the International Congress of Actuaries, Helsinki, 1988. This discusses various "stabilizers" and "fail-safe mechanisms" that could be embodied in such systems. He also sent me a copy of his May 28, 1988 "Statement to the Subcommittee on Social Security and Family Policy, Committee on Finance, U.S. Senate, on Long-Term Status of Social Security Trust Funds". In this statement, he projects a series of DASDI tax rates under which fund ratios would slowly increase to 100% before year 2,000 and would remain at that level thereafter. Thereby, the "roller-coaster" effect under present law would be eliminated.

Ralph Edwards, James Hickman, Robert Myers and Charles Trowbridge raise questions about the practicality of $i_p(k)$, and the relation of $i_{1,P}(k)$ to the market rates of interest. It should be realized that the impact of nuclear holocaust hazard is universal on all rational financial transactions (except perhaps very short-term), thereby bringing pressure for higher investment return for lenders, and higher capital costs for borrowers. The additional investment return is then available for supplementing the discounted reserves held to meet the requirements of financial security systems. These remarks are related to Ralph Edwards' annuity illustration, and to formula (4.3) of the paper. Both he and I are reaching the conclusion that $i_{1,2}(k) = i_1(k) + i_2(k) + i_1(k)i_2(k)$ must be the market rate of investment return. In that sense, recognition of nuclear holocaust hazard need not disturb daily actuarial operations but, in my opinion, actuarial science should consider such hazard and its effects. But I also understand James Hickman's haunting impression that an actuarial

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model is not the most comprehensive way to think about the unthinkable. Nevertheless, such models are fascinating and illuminating for me, and may eventually engage the attention of others. By the way, I conjecture that $i_2(k)$ could be used to model inflation but in a different sense than for its use with nuclear holocaust hazard.

My thanks are due to the readers I have mentioned and also to John Beekman, John Boermeester, Marjorie Butcher and Donald Jones for their encouragement and noting of errata.

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